

1 Express  $6 \cos 2\theta + \sin \theta$  in terms of  $\sin \theta$ .

Hence solve the equation  $6 \cos 2\theta + \sin \theta = 0$ , for  $0^\circ \leq \theta \leq 360^\circ$ . [7]

2 (i) Show that  $\cos(\alpha + \beta) = \frac{1 - \tan \alpha \tan \beta}{\sec \alpha \sec \beta}$ . [3]

(ii) Hence show that  $\cos 2\alpha = \frac{1 - \tan^2 \alpha}{1 + \tan^2 \alpha}$ . [2]

(iii) Hence or otherwise solve the equation  $\frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} = \frac{1}{2}$  for  $0^\circ \leq \theta \leq 180^\circ$ . [3]

3 Given the equation  $\sin(\theta + 45^\circ) = 2 \cos \theta$ , show that  $\sin \theta + \cos \theta = 2 \cos \theta$ . Hence

solve, correct to 2 decimal places, the equation for  $0^\circ \leq \theta \leq 360^\circ$ .

$\leq \leq$  [6]

4 Solve the equation  $\tan(\theta + 45^\circ) = 1 - 2 \tan \theta$ , for  $0^\circ \leq \theta \leq 90^\circ$ . [7]

5 Given that  $\sin(\theta + \alpha) = 2 \sin \theta$ , show that  $\tan \theta = \frac{\sin \alpha}{2 - \cos \alpha}$ .

Hence solve the equation  $\sin(\theta + 40^\circ) = 2 \sin \theta$ , for  $0^\circ \leq \theta \leq 360^\circ$ . [7]

6 Solve the equation  $2 \cos 2x = 1 + \cos x$ , for  $0^\circ \leq x < 360^\circ$ . [7]